

Assignment One

Linear Algebra

Class _____ Name _____ Score _____

1. Consider the matrices

$$A = \begin{pmatrix} 3 & 0 \\ -1 & 2 \\ 1 & 1 \end{pmatrix}, B = \begin{pmatrix} 4 & -1 \\ 0 & 2 \end{pmatrix}, C = \begin{pmatrix} 1 & 4 & 2 \\ 3 & 1 & 5 \end{pmatrix}$$

$$D = \begin{pmatrix} 1 & 5 & 2 \\ -1 & 0 & 1 \\ 3 & 2 & 4 \end{pmatrix}, E = \begin{pmatrix} 6 & 1 & 3 \\ -1 & 1 & 2 \\ 4 & 1 & 3 \end{pmatrix}$$

Compute

(a) $-3(D + 2E)$ (b) $D^T - E^T$ (c) $(AB)C$

2. Consider the matrices

$$A = \begin{pmatrix} 3 & 4 & 1 \\ 2 & -7 & -1 \\ 8 & 1 & 5 \end{pmatrix}, B = \begin{pmatrix} 8 & 1 & 5 \\ 2 & -7 & -1 \\ 3 & 4 & 1 \end{pmatrix}, C = \begin{pmatrix} 3 & 4 & 1 \\ 2 & -7 & -1 \\ 2 & -7 & 3 \end{pmatrix}$$

Find elementary matrices E_1, E_2 such that

$$E_1A = B, E_2A = C$$

3. Find the inverse of the following matrices, and check your answer by multiplication.

$$(a) \begin{pmatrix} 3 & 4 & -1 \\ 1 & 0 & 3 \\ 2 & 5 & -4 \end{pmatrix} \quad (b) \begin{pmatrix} 1 & 0 & 1 \\ 0 & 1 & 1 \\ 1 & 1 & 0 \end{pmatrix}$$

4. Solve

$$(a) \begin{cases} x_1 - x_2 + 5x_3 - x_4 = 0 \\ x_1 + x_2 - 2x_3 + 3x_4 = 0 \\ 3x_1 - x_2 + 8x_3 + x_4 = 0 \\ x_1 + 3x_2 - 9x_3 + 7x_4 = 0 \end{cases} \quad (b) \begin{cases} x_1 + x_2 - 3x_3 - x_4 = 1, \\ 3x_1 - x_2 - 3x_3 + 4x_4 = 4, \\ x_1 + 5x_2 - 9x_3 - 8x_4 = 0, \end{cases}$$